

**0.089" metering orifice test  
January 26th, 2005**

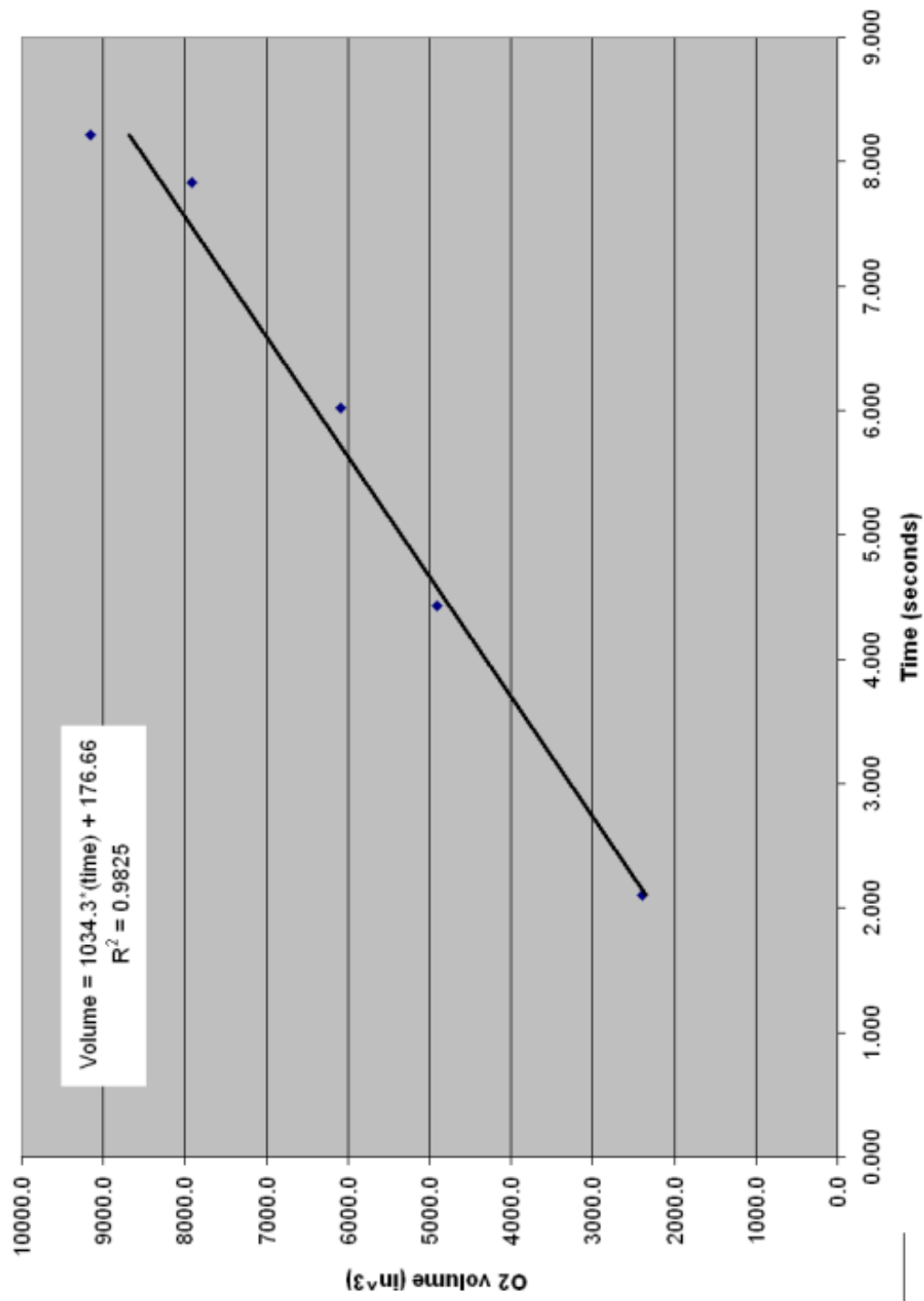
**GIVEN**

Inlet	302	PSI
Outlet	130	PSI
Room Temp	60	F
Barrel Circumference	69.38	inches (outside)
Barrel Wall Thickness	0.125	inches
Barrel Wall height	33.09	inches (average )

**DATA**

Trial #	Duration (seconds)	Side 1 height (from top in inches)	Side 2 height (from top in inches)	Average height (inches)	O2 column height (inches)	O2 Volume (in <sup>3</sup> )	Flow Rate (in <sup>3</sup> /s)
1	8.216	8.50	8.75	8.63	24.47	9160.4	1114.9
2	6.024	16.75	16.88	16.81	16.28	6094.8	1011.7
3	4.434	19.88	20.13	20.00	13.09	4901.3	1105.4
4	2.100	26.63	26.75	26.69	6.40	2397.3	1141.6
5	7.836	11.88	12.00	11.94	21.15	7920.1	1010.7
Barrel I.D (inches)		21.8343					

**.089" Metering Orifice**



## Calculate transferred O2 volumetric flow rate

Find the oxygen flow rate through a specific diameter metering orifice at a given upstream pressure.

Given :	$C_d := 1.096$	Flat plate metering orifice
	$P_{atm} := 14.7\text{psi}$	
	$P_{atm} = 1.014 \times 10^5 \text{ Pa}$	Atmospheric pressure
	$P_{inlet} := 1000\text{psi}$	
	$P_{inlet} = 6.895 \times 10^6 \text{ Pa}$	Upstream pressure
	$A_1 := \frac{\pi \cdot (.089\text{in})^2}{4}$	
	$A_1 = 4.014 \times 10^{-6} \text{ m}^2$	Metering orifice area t
	$R := 260 \frac{\text{J}}{\text{kg} \cdot \text{K}}$	Gas constant for oxygen
	$\gamma := 1.4$	ratio of specific heats for oxygen
	$T_1 := 288.71\text{K}$	Gas temperature (60F)

$$q := C_d \cdot A_1 \cdot P_{inlet} \cdot \sqrt{\frac{\gamma}{R \cdot T_1} \cdot \left(\frac{2}{1 + \gamma}\right)^{\frac{\gamma+1}{2\gamma-2}}}$$

$$q = 0.0758 \frac{\text{kg}}{\text{s}}$$

$$V_{dot} := \frac{q \cdot R \cdot T_1}{P_{atm}}$$

$$V_{dot} = 0.056 \frac{\text{m}^3}{\text{s}}$$

$$V_{dot} = 118.953 \frac{\text{ft}^3}{\text{min}}$$

## Metering orifice (.089" dia)

Given :

$$\dot{m}_{\text{O}_2} := .0758 \frac{\text{kg}}{\text{s}}$$

$$m_{\text{paraffin}} := .1804 \text{kg} \quad \text{from spreadsheet ( mass paraffin consumed at 7 seconds given } \dot{m} \text{)}$$

$$T_{\text{burn}} := 7 \text{s}$$

$$I_{\text{sp}} := 210 \text{s}$$

Then

$$m_{\text{O}_2} := \dot{m}_{\text{O}_2} \cdot T_{\text{burn}}$$

$$m_{\text{O}_2} = 0.531 \text{ kg}$$

$$m_{\text{propellant}} := m_{\text{O}_2} + m_{\text{paraffin}}$$

$$m_{\text{propellant}} = 0.711 \text{ kg}$$

Calculate average thrust from burned propellants

$$\text{Thrust} := \frac{m_{\text{propellant}} \cdot g \cdot I_{\text{sp}}}{T_{\text{burn}}}$$

$$\text{Thrust} = 209.176 \text{ N}$$

$$\text{Thrust} = 47.025 \text{ lbf}$$

Oxidizer to fuel ration

$$\text{OF} := \frac{m_{\text{O}_2}}{m_{\text{paraffin}}}$$

$$\text{OF} = 2.941$$